

DANIEL GRIN Haverford College IAS informal seminar December 15, 2016 

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Dark matter?

Dark matter?

Decays and generates...

Baryon #

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OUTLINE

*****Ultra-light axions

*Motivation, observational imprint, tools

*Constraints

*Future work

*Curvaton-sourced isocurvature perturbations

*Linearly observable isocurvature

*Compensated isocurvature perturbations

WHAT ARE AXIONS?



New scalar field with global U(1) symmetry! Broken at scale f_a

$$\mathcal{L}_{\rm CPV} = \frac{\theta g^2}{32\pi^2} G\tilde{G} - \frac{a}{f_{\rm a}} g^2 G\tilde{G}$$
$$m_a \sim \frac{\Lambda_{\rm QCD}^2}{f_a}$$

 \mathcal{A}

* Field misaligned $m_a \gg 3H \rightarrow \text{oscillation}$

 $* \rho_a \propto (1+z)^3$ [as cold dark matter should]

Peccei + Quinn (1977), Weinberg +Wilczek (1978), Kim (1979), Zhitnitsky (1980), Dine et al. (1981), Sikivie (1982, 1983, 1985,1986, and many others!)

WHAT ARE AXIONS?



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 \mathcal{A}

$$\Omega_{\rm mis}h^2 = 0.236 \left\langle \theta_i^2 f(\theta_i) \right\rangle \left(\frac{m_a}{6.2\mu {\rm eV}} \right)^{-7/6}$$

Dn

d

Peccei + Quinn (1977), Weinberg +Wilczek (1978), Kim (1979), Zhitnitsky (1980), Dine et al. (1981), Sikivie (1982, 1983, 1985,1986, and many others!)

LIMITS



LIMITS

Cosmological dark matter



* In string theory, extra dimensions compactified: Calabi-Yau manifolds



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Hundreds of scalars with approx shift symmetry Many axions

* Mass acquired non-perturbatively (instantons, D-Branes)

$$m_a^2 = \frac{\mu^4}{f_a^2} e^{-\text{Volume}}$$

* In string theory, extra dimensions compactified: Calabi-Yau manifolds









Hundreds of scalars with approx shift symmetry Many axions

* Mass acquired non-perturbatively (instantons, D-Branes) Scale of new ultra-violet physics $m_a^2 = \frac{\mu^4}{f^2} e^{-\text{Volume}}$

* In string theory, extra dimensions compactified: Calabi-Yau manifolds







Hundreds of scalars with approx shift symmetry Many axions

* Mass acquired non-perturbatively (instantons, D-Branes)

Scale of extra dimensions $m_a^2 = \frac{\mu^4}{f_a^2} e^{-\text{Volume}}$ in Planck units

* In string theory, extra dimensions compactified: Calabi-Yau manifolds







Axiverse! Arvanitaki+ 2009 Witten and Srvcek (2006), Acharya et al. (2010), Cicoli (2012)



Testing ultra-light axions with cosmology

$$10^{-33} \text{ eV} < m_a < 10^{-18} \text{ eV}$$







$$m \ll 3H \rightarrow n_a \propto \text{ const}, w_a \equiv \frac{P_a}{\rho_a}, w_a \simeq -1$$

$$m \gg 3H \rightarrow n_a \propto a^{-3}, \langle w_a \rangle_{T=2\pi/m_a} = 0$$



 $m \ll 3H \rightarrow n_a \propto \text{ const}, w_a \equiv \frac{P_a}{\rho_a}, w_a \simeq -1$

$$m \gg 3H \to n_a \propto a^{-3}, \langle w_a \rangle_{T=2\pi/m_a} = 0$$



For QCD axion, we have a CDM candidate!

$$\Omega_{\rm mis}h^2 = 0.236 \left\langle \theta_i^2 f(\theta_i) \right\rangle \left(\frac{m_a}{6.2\mu {\rm eV}} \right)^{-7/6}$$

Different parameter space for non-QCD axion(Frieman et al 1995, Coble et al. 2007)



 $10^{-33} \text{ eV} < m_a < 10^{-18} \text{ eV}$

 $\Omega_a \propto \left(f_a\overline{ heta}
ight)^2 \sqrt{m_a}$

Different parameter space for non-QCD axion(Frieman et al 1995, Coble et al. 2007)



$$10^{-33} \text{ eV} < m_a < 10^{-18} \text{ eV}$$

$$a \equiv a_{\rm osc} \quad m_a = 3H(a)$$

Different parameter space for non-QCD axion(Frieman et al 1995, Coble et al. 2007)





`DM' axions

$$a_{
m osc} < a_{
m eq}$$
 Oscillation starts in time for struct. formation $m_a > 10^{-27}~{
m eV}$

DE axions

Oscillation starts too late for struct. formation $a_{\rm osc} > a_{\rm eq}$ $m_a < 10^{-27} \text{ eV}$

GROWTH OF ULA PERTURBATIONS

*Perturbed Klein-Gordon + Gravity

 $\ddot{\delta\phi} + 2\mathcal{H}\delta\dot{\phi} + (k^2 + m_a^2 a^2)\delta\phi = 4\dot{\Psi}\dot{\phi_0} - \Psi a^2 m_a^2\phi_0$

*Axionic Jeans Scale is macroscopic [in contrast to QCD axion]:

$$\lambda_J = 2.4 h^{-1/2} \left(\frac{m}{10^{-25} \text{ eV}} \right)^{-1/2} \text{ Mpc}$$

*Computing observables is expensive for $m \gg 3\mathcal{H}$:

* Coherent oscillation time scale $\Delta \eta \sim (ma)^{-1} \ll \Delta \eta_{\text{CAMB}}$

* WKB approximation

 $\delta\phi = A_c \Delta_c(k,\eta) \cos\left(m\eta\right) + A_s \Delta(k,\eta) \sin\left(m\eta\right)$

$$c_a^2 = \frac{\delta P}{\delta \rho} = \frac{k^2 / (4m^2 a^2)}{1 + k^2 / (4m^2 a^2)}$$

Growth of **ULA** perturbations





*Modes with $k \gg k_{\rm J} \sim \sqrt{m\mathcal{H}}$ oscillate instead of growing

AXIONCAMB

CMB and matter perturbation code including ULAs!



ULA of any mass is self-consistently followed from DE to DM regime

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AXIONCAMB

Code by Grin et al. 2013, based on CAMB (A. Lewis) <u>http://github.com/dgrin1/axionCAMB</u>

Please download, comment, test, poke, and improve it!

ULAS AS DARK ENERGY AND THE ANGULAR SOUND HORIZON

D (sensitive to any energy source)



ULAS AS DARK ENERGY AND THE ANGULAR SOUND HORIZON

D (sensitive to any energy source)



ULAS AS DARK ENERGY AND THE ANGULAR SOUND HORIZON



Faster early expansion brings LSS closer

ULAS AS DARK ENERGY





ULAs and the CMB: high mass and early ISW *Higher mass (DM-like) case: high-l ISW*



CMB temperature anisotropies from potential decay $\Delta T_{\rm ISW} = -2 \int_0^{\eta_{\rm dec}} d\eta \dot{\Phi}(\eta, \hat{n}\eta)$

ULAs and the CMB: high mass and early ISW *Higher mass (DM-like) case: high-l ISW*



CMB temperature anisotropies from potential decay $\Delta T_{\rm ISW} = -2 \int_0^{\eta_{\rm dec}} d\eta \dot{\Phi}(\eta, \hat{n}\eta)$

ULAs and the CMB: high mass and early ISW *Higher mass (DM-like) case: high-l ISW*



Radiation pressure causes potential decay



 $\Delta \overline{P\Delta A} > \rho \delta V \nabla \overline{\Phi}$
ULAs and the CMB: high mass and early ISW *Higher mass (DM-like) case: high-l ISW*



Matter power spectrum for ULA (in DM regime)



*DM perturbation growth severely suppressed if $k > k_J \simeq \sqrt{m\mathcal{H}}$

*Suppression
$$\propto -\frac{\Omega_a}{\Omega_a + \Omega_c}$$

*Analogous to effect of neutrinos

Matter power spectrum for ULA (in DM regime)





*DM perturbation growth severely suppressed if $k > k_J \simeq \sqrt{m\mathcal{H}}$

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$$\propto -\frac{\Omega_a}{\Omega_a + \Omega_c}$$

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DATA + ANALYSIS





*Planck 2013 temperature anisotropy power spectra (+SPT+ACT) *Cosmic variance limited to $\ell \sim 1500$

*WiggleZ galaxy survey (linear scales only $k \leq 0.2h \ {
m Mpc}^{-1}$)

*240,000 emission line galaxies at z<1

*3.9 m Anglo-Australian Telescope (AAT)

*Nested sampling, MCMC, vary $m_a, \Omega_a h^2, \Omega_c h^2, \Omega_b h^2, \Omega_\Lambda, n_s, A_s, \tau_{reion}$



CONSTRAINTS

Comparison with data





R.Hlozek, DG, D.J. E. Marsh, P.Ferreira

arXiv:1410.2896, Phys. Rev. D 91, 103512 (2015) arXiv:1403.4216, Phys. Rev. Lett. 113, 011801 (2014) arXiv:1303.3008, Phys. Rev. D 87, 121701(R) (2013)



CONSTRAINTS



*Tight constraints over 7 orders of magnitude in mass:

Thanks to AXICAMB and Planck

*ULAs are viable DM/DE candidates in linear theory outside ``belly'' 16

What's next?

FUTURE WORK: ULAS CORES + CUSPS?



Cores! (Hu/Gruzinov/Barkana 2001, see also Marsh and Silk 2013, Marsh and Pop 2015, Matos 2012, Schive 2014, and others)

FUTURE WORK: ULAS CORES + CUSPS?



From Schive et al., more cosmological volume needed for statistics, baryons, etc...

Future work: ulas and galaxies

Missing satellite problem?



Hui, Ostriker, Tremaine and Witten 2016 Marsh et al 2014, Klypin 1999, Bullock 2010 Dynamical friction, tidal disruption, substructure, FDM disks?, globular cluster orbits in Fornax dwarf, halo model, spherical collapse, better simulations (much work to be done!)

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*Hard switch from scalar-field evolution (KG equation) to 0th-order WKB (fluid) description

 $m \gg 3\mathcal{H}$ $\delta \phi = A_c \Delta_c(k,\eta) \cos(m\eta) + A_s \Delta(k,\eta) \sin(m\eta)$

$$c_a^2 = \frac{\delta P}{\delta \rho} = \frac{k^2 / (4m^2 a^2)}{1 + k^2 / (4m^2 a^2)}$$

*Real mode functions not sines and cosines!

*Corrections to WKB near match-point





$$c_s^2 = \frac{k^2/(4m_a^2a^2)}{1+k^2/(4m_a^2a^2)} + \left(\frac{\mathcal{H}}{m_a}\right)^2 g(k,\eta,m_a)$$

Work in progress, J. Cookmeyer HC 2017



Work in progress, J. Cookmeyer HC 2017





Work in progress, J. Cookmeyer HC 2017



CMB-S4



From CMB-S4 Science book.... arXiv: 1610.02743

FUTURE WORK: CMB LENSING

A slice of (dark matter) life at $z\sim 1$





FUTURE WORK: CMB LENSING

A slice of (dark matter) life at $z\sim 1$





Future work: CMB lensing

A slice of (dark matter) life at $z\sim 1$





$$\kappa(\vec{\theta}) = \frac{1}{2} \nabla_{\vec{\theta}}^2 \psi(\vec{\theta}) = \frac{1}{2} \vec{\nabla} \cdot \vec{\alpha}$$

Deflection angle

$$\psi(\vec{\theta}) = \frac{2d_c(\eta_{ls})}{d_c(\eta_l)d_c(\eta_s)} \int \Phi(d_c(\eta)\theta, \eta)d\eta$$

Future work: CMB lensing

A slice of (dark matter) life at $z\sim 1$





 $\kappa(\vec{\theta}) = \frac{1}{2} \nabla_{\vec{\theta}}^2 \psi(\vec{\theta}) = \frac{1}{2} \vec{\nabla} \cdot \vec{\alpha} \quad \text{Deflection angle}$ $\psi(\vec{\theta}) = \frac{2d_c(\eta_{ls})}{d_c(\eta_l)d_c(\eta_s)} \int \Phi(d_c(\eta)\theta, \eta)d\eta$ **ULAs** change

Future work: CMB lensing

ULA saturating TT-only limits falsifiable at 4.5σ



S4-CAST FOR LENSING AND ULAS





Fisher forecast using OXFISH code—OOM improvement drive by lensing

arXiv: 1607.08208

R.Hlozek, D.J.E. Marsh, D.G., J. Dunkley, R. Allison, E. Calabrese

AXIONS AND ISOCURVATURE

* If PQ symmetry broken during/before inflation

$$\sqrt{\langle a^2 \rangle} = \frac{H_{\rm I}}{2\pi}$$

 $f_a > H_I$

Quantum zero-point fluctuations!

*Subdominant species seed isocurvature fluctuations

$$\zeta \propto \frac{\rho_a}{\rho_{\rm tot}} \frac{\delta \rho_a}{\rho_a} \ll 10^{-5}$$

$$S_{a\gamma} = \frac{\delta n_a}{n_a} - \frac{\delta n_\gamma}{n_\gamma} = \frac{\delta \rho_a}{\rho_a} - \frac{3}{4} \frac{\delta \rho_\gamma}{\rho_\gamma} = 2\frac{\delta a}{a} \sim 10^{-5}$$

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Related to axion abundance

$$S_{a\gamma} = \frac{\delta n_a}{n_a} - \frac{\delta n_\gamma}{n_\gamma} = \frac{\delta \rho_a}{\rho_a} - \frac{3}{4} \frac{\delta \rho_\gamma}{\rho_\gamma} = 2 \frac{\delta a}{a} \sim 10^{-5}$$

Adiabatic



Neutrinos CDM Photons Baryons

 δn_{γ} δn_i S_i n_{γ} n_i



 $ds^{2} = a^{2}(\eta) \left\{ -(1+2\Phi) d\eta^{2} + (1-2\Phi) dx^{i} dx_{j} \right\} _{26}$

Baryon isocurvature $S_b \neq 0 \Delta \Phi = 0$

Neutrinos CDM Photons Baryons

 δn_i δn_{γ} S_i n_{γ} $\overline{n_i}$

 $\nabla^2 \Phi = 4\pi G \delta \rho$

 $ds^{2} = a^{2}(\eta) \left\{ -(1+2\Phi) d\eta^{2} + (1-2\Phi) dx^{i} dx_{j} \right\} _{26}$

isocurvature

Neutrinos CDM Photons Baryons

 $S_c \neq 0 \ \Delta \Phi = 0$

$$S_i = \frac{\delta n_i}{n_i} - \frac{\delta n_\gamma}{n_\gamma}$$

 $\nabla^2 \Phi = 4\pi G \delta \rho$

 $ds^{2} = a^{2}(\eta) \left\{ -(1+2\Phi) d\eta^{2} + (1-2\Phi) dx^{i} dx_{j} \right\}_{26}$

ν isocurvature \checkmark

Neutrinos CDM Photons Baryons

$S_{\nu} \neq 0 \quad \Delta \Phi = 0$

$$S_i = \frac{\delta n_i}{n_i} - \frac{\delta n_\gamma}{n_\gamma}$$

 $\nabla^2 \Phi = 4\pi G \delta \rho$

 $ds^{2} = a^{2}(\eta) \left\{ -(1+2\Phi) d\eta^{2} + (1-2\Phi) dx^{i} dx_{j} \right\}_{26}$

 $\begin{array}{c}
\nu \\
\text{isocurvature} \\
S_{\nu} \neq 0 \\
\end{array}
\begin{array}{c}
\text{Neutrinos} \\
\text{CDM} \\
\text{Photons} \\
\text{Baryons}
\end{array}$

All density initial conditions can be expressed in terms of these! These conditions are not conserved under fluid evolution

Initial conditions determine dynamics for a linear system $_{26}$

CMB POWER SPECTRA



From arXiv: 1303.5082 (Planck inflation paper)

ULAS AND ISOCURVATURE FLUCTUATIONS



Spectra from AXIONCAMB using initial conditions obtained in DG+ (2015 in prep)

ULAS AND ISOCURVATURE FLUCTUATIONS

Planck 2015 TT



$$\begin{aligned} \alpha &\equiv \frac{P_{S_{c\gamma}}(k)}{P_{S_{c\gamma}(k)} + P_{\mathcal{R}}(k)} \leq 0.039 \\ \alpha &\propto \left(\frac{H_I}{f_a \overline{\theta}}\right)^2 \quad \Omega_a \propto \left(f_a \overline{\theta}\right)^2 \sqrt{m_a} \end{aligned}$$

ULAS AND ISOCURVATURE FLUCTUATIONS

Planck 2015 TT



D.J.E. Marsh, DG +, arXiv:1403.4216, Phys. Rev. Lett. 113, 011801 D.J.E. Marsh, DG +, arXiv:1303.3008, Phys. Rev. D 87, 121701(R)

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HIGH-ENERGY COSMOLOGY WITH AXION ISOCURVATURE



From CMB-S4 Science book.... arXiv: 1610.02743



CURVATON MODEL





some schematics from Wands, Enqvist, Lyth, Takahashi (2012-2015)

* Hard for an inflationary model to do everything you want $\frac{k^3 P_{\mathcal{R}}(k)}{2\pi^2} = \frac{H_k^2}{8\pi^2 M_{\rm pl}^2 \epsilon} \quad \epsilon = \frac{M_{\rm pl}^2}{2} \left(\frac{V'}{V}\right)^2$

* Curvaton' σ is a spectator (sub-dominant) during inflation * After reheating, σ decays with

$$r_{\rm D} \equiv \frac{\rho_{\sigma}}{\rho_{\sigma} + (4/3)\,\rho_{\rm RAD}}$$

Many curvaton candidates (e.g. sneutrino from MSSM, axion, generic modulus) 30

CURVATURE PERTURBATIONS IN CURVATON MODEL

*Curvaton becomes more important once $m_{\sigma} \gg H$, $\rho_{\sigma} \propto a^{-3}$ *Inflationary curvature perts assumed negligible

$$\zeta = \frac{r_{\rm D}\delta_{\rho_{\sigma}}}{3}$$

*3 possibilities for curvaton decay products

 $\delta_x = \begin{cases} 0 & \text{if } x \text{ produced before curvaton decay} \\ \frac{3}{r_{\rm D}}\zeta & \text{if } x \text{ produced by curvaton decay} \\ 3\zeta & \text{if } x \text{ produced after curvaton decay} \end{cases}$

Mismatch for species produced before, by curvaton decay



Totally (or anti) correlated with density field

Lyth, Wands, Ungarelli (2002-2003) 2002, Malik and Lyth 2006 Mollerach 1990, Moroi and Takahashi 2001 21

NEUTRINO ISOCURVATURE IN THE CURVATON MODEL

* Weak interactions convert lepton number to neutrino density

* There could be lepton asymmetry (carries to neutrinos)

$$f_{i\in\{\nu_{e},\nu_{\tau},\nu_{\mu}\}}^{\pm} = \left[e^{E/T_{i}} + 1\right]^{-1}$$

* Neutrino isocurvature generated if lepton number produced by curvaton decay

$$\delta_{\nu} \neq \delta_{\gamma} \qquad S_{\nu\gamma} \neq 0$$

* Modified relationship between relativistic species and total curvature

$$\zeta = (1 - R_{\nu})\frac{\delta_{\gamma}}{4} + R_{\nu}\frac{\delta_{\nu}}{4}$$
NEUTRINO ISOCURVATURE IN THE CURVATON MODEL

* Variety of lepton number generation scenarios

* Affleck/Dine leptogenesis (L-generation by curvaton decay)

$$S_{\nu\gamma} = \frac{135}{7} \left(\frac{\xi_{\rm lep}}{\pi}\right)^2 \left(\frac{1}{r_{\rm D}} - 1\right) \zeta$$

PANOPLY OF DECAY SCENARIOS

* Project: T.L. Smith + DG, systematically explore all 27 decay scenarios arXiv: 1511.07431, Phys. Rev. D 94 103517

scenario	$rac{S_{b\gamma}}{\zeta}$	$rac{S_{c\gamma}}{\zeta}$	$rac{S_{m\gamma}}{\zeta}$
$(b_{ m by}, c_{ m before}, L_{y_L})$	$3\left(\frac{1}{r_D} - 1\right) + R_{\nu}\frac{S_{\nu\gamma}}{\zeta}$	$-3 + R_{\nu} \frac{S_{\nu\gamma}}{\zeta}$	$3\left(\frac{\Omega_b}{\Omega_m r_D} - 1\right) + R_{\nu} \frac{S_{\nu\gamma}}{\zeta}$
$(b_{ m before}, c_{ m by}, L_{y_L})$	$-3 + R_{ u} \frac{S_{ u\gamma}}{\zeta}$	$3\left(\frac{1}{r_D} - 1\right) + R_{\nu}\frac{S_{\nu\gamma}}{\zeta}$	$3\left(\frac{\Omega_c}{\Omega_m r_D} - 1\right) + R_{\nu} \frac{S_{\nu\gamma}}{\zeta}$
$(b_{ m by}, c_{ m after}, L_{y_L})$	$3\left(\frac{1}{r_D} - 1\right) + R_{\nu}\frac{S_{\nu\gamma}}{\zeta}$	$R_{ u}rac{S_{ u\gamma}}{\zeta}$	$3rac{\Omega_b}{\Omega_m}\left(rac{1}{r_D}-1 ight)+R_ urac{S_{ u\gamma}}{\zeta}$
$(b_{ m after}, c_{ m by}, L_{y_L})$	$R_{ u}rac{S_{ u\gamma}}{\zeta}$	$3\left(\frac{1}{r_{\rm D}}-1\right) + \frac{S_{b\gamma}}{\zeta}$	$3\frac{\Omega_c}{\Omega_m}\left(\frac{1}{r_D}-1\right) + R_{\nu}\frac{S_{\nu\gamma}}{\zeta}$
$(b_{ ext{before}}, c_{ ext{arter}}, L_{u_L})$	$-3 + R_{\nu} \frac{S_{\nu\gamma}}{\zeta}$	$R_{\nu}\frac{S_{\nu\gamma}}{\zeta}$	$-3rac{\Omega_b}{\Omega_m}+R_ urac{S_{ u\eta}}{\zeta}$
$(b_{\mathrm{after}}, c_{\mathrm{before}}, L_{y_L})$	$R_{\nu} \frac{S_{\nu\gamma}}{\zeta}$	$-3 + \frac{S_{b\gamma}}{\zeta}$	$-3\frac{\Omega_c}{\Omega_m} + R_\nu \frac{S_{\nu\gamma}}{\zeta}$
$(b_{ ext{before}}, c_{ ext{before}}, L_{y_L})$	$-3 + R_{\nu} \frac{S_{\nu\gamma}}{\zeta}$	$rac{S_{b\gamma}}{\zeta}$	$rac{S_{b\gamma}}{\zeta}$
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$(b_{\mathrm{after}}, c_{\mathrm{after}}, L_{y_L})$	$R_{ u}rac{S_{ u\gamma}}{\zeta}$	$R_{ u}rac{S_{ u\gamma}}{\zeta}$	$R_{ u}rac{S_{ u\gamma}}{\zeta}$



Compensated scenarios



* Allowed parameter space for compensated scenarios:

* baryon/CDM entropy fluctuations $S_{bc} \propto \zeta \neq 0$ More on this soon.... stay tuned!

Compensated scenarios: enhanced lepton constraints



* Compare with
$$\xi_{\text{lep}}^2 \leq 0.3$$
 from N_{eff} only

* Unavoidable neutrino isocurvature when matter isocurvature nearly vanishes

$$S_{\nu\gamma} = \frac{135}{7} \left(\frac{\xi_{\rm lep}}{\pi}\right)^2 \left(\frac{1}{r_{\rm D}} - 1\right) \zeta$$

* "Nuisance" mode identified (Lewis 2002)

Compensated Isocurvature Perturbation (CIP)

$$\delta_{\rm b}^{\rm CIP} = \Delta(\hat{n}, \eta) \quad \delta_{\rm c}^{\rm CIP} = -\frac{\Omega_c}{\Omega_{\rm b}} \Delta(\hat{n}, \eta), \quad \delta\rho_{\rm b}^{\rm CIP} + \delta\rho_{\rm c}^{\rm CIP} = 0$$

Baryon-dark matter 'entropy'
$$\mathcal{S}_{\rm bc} = \frac{\delta n_{\rm b}}{n_{\rm b}} - \frac{\delta n_{\rm c}}{n_{\rm c}} \neq 0$$

* Subdominant fluctuations: Adiabatic modes dominate, but do the relative number densities of DM and baryons fluctuate?

BARYON-DM ISOCURVATURE

* "Nuisance" mode identified (Lewis 2002)

Neutrinos CDM Photons Baryons

Compensated Isocurvature Perturbation (CIP)

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BARYON-DM ISOCURVATURE

* "Nuisance" mode identified (Lewis 2002)

Adiabatic

Neutrinos CDM Photons Baryons

Compensated Isocurvature Perturbation (CIP)

* Subdominant fluctuations: Adiabatic modes dominate, but do the relative number densities of DM and baryons fluctuate?

WHY DIDN'T ANYONE NOTICE?

* *Observationally null in the CMB!* (surprising but true, only at linear order!)

 $\Delta P = 0$ if

$$\lambda > \lambda_J \sim \frac{c_{s,b}}{H} \sim \frac{c}{H} \sqrt{\frac{k_B T_b}{m_p}} \to \ell \gtrsim 10^5$$



* Baryon terms in photon equations ... $\propto \overline{n}_e \sigma_T (1 + \delta_b) \nabla \cdot \vec{v}_b$



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* Baryon terms in photon equations ... $\propto \overline{n}_e \sigma_T (1 + \delta_b) \nabla \cdot \vec{v}_b$

higher order effect ... neglected in first-order Boltzmann codes

* Acoustic horizon scale modulated by CIPs

* Baryon-photon sound speed depends on electron density

$$c_s^2 = \frac{1}{3} \left[1 + 3\rho_{\rm b}/4\rho_{\gamma} \right]^{-1}$$

* Damping scale modulated by CIPs



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* Polarization : $\Delta(\hat{n})$ affects T_{2i} generation and n_e $Q, U \propto \int n_e(\eta) \left[1 + \Delta(\hat{n})\right] T_{2i}(\eta, \hat{n}) d\eta$





CMB detectability of CIPs shown in arXiv: 1107.1716- Phys. Rev. Lett. 107 261301, DG+ arXiv: 1107.5047- Phys. Rev. D. 84 123003, DG+

* Power spec. results were true, averaging over realizations of primordial $\Phi(\hat{n})$ and CIP amplitude $\Delta(\hat{n})$



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- * In single realization of CIP spec., a long wavelength CIP w/ amp Δ_{LM} modulates the power spectrum across the sky







- * Power spec. results were true, averaging over realizations of primordial $\Phi(\hat{n})$ and CIP amplitude $\Delta(\hat{n})$
- * In single realization of CIP spec., a long wavelength CIP w/ amp Δ_{LM} modulates the power spectrum across the sky



*Heuristically:

- 1. Tile all-sky map with patches
- 2. Measure power spec in each patch
- 3. Reconstruct $\Delta(\hat{n})$

$$T(\vec{\theta})_{\rm CIP} = T(\vec{\theta})_{\rm no\ CIP} + \left. \frac{dT(\vec{\theta})_{\rm no\ CIP}}{d\Omega_b} \right|_{\Omega_m} \Delta(\vec{\theta})$$

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$$T(\vec{\theta})_{\rm CIP} = T(\vec{\theta})_{\rm no\ CIP} + \frac{dT(\theta)_{\rm no\ CIP}}{d\Omega_b} \bigg|_{\Omega_m} \Delta(\vec{\theta})$$
$$T(\vec{l})_{\rm CIP} = T(\vec{l})_{\rm no\ CIP} + \int d\vec{L} \frac{dT(\vec{L} - \vec{l})_{\rm no\ CIP}}{d\Omega_b} \bigg|_{\Omega_m} \Delta(\vec{\theta})$$

$$\left\langle T\left(\vec{l}\right)_{\rm CIP} T^*\left(\vec{l'}\right)_{\rm CIP} \right\rangle = (2\pi)^2 C_l^{TT} \delta^{(2)} (\vec{l} - \vec{l'}) + (2\pi)^2 \Delta (\vec{l} + \vec{l'}) \left. \frac{dC_{l'}^{TT}}{d\Omega_b} \right|_{\Omega_m}$$

 (\vec{L})

There in standard cosmology

 $\Delta(\vec{\theta})$

$$T(\vec{\theta})_{\rm CIP} = T(\vec{\theta})_{\rm no\ CIP} + \frac{dT(\vec{\theta})_{\rm no\ CIP}}{d\Omega_b} \bigg|_{\Omega_m} \Delta(\vec{\theta})$$
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Isotropy-breaking term in fixed **CIP** realization

 $\Delta(\vec{\theta})$

$$T(\vec{l})_{\rm CIP} = T(\vec{l})_{\rm no\ CIP} + \int d\vec{L} \left. \frac{dT(\vec{L} - \vec{l})_{\rm no\ CIP}}{d\Omega_b} \right|_{\Omega_m} \Delta(\vec{L})$$

 $T(\vec{\theta})_{\rm CIP} = T(\vec{\theta})_{\rm no \ CIP} + \frac{dT(\vec{\theta})_{\rm no \ CIP}}{d\Omega_{\rm b}}$

$$\left\langle T\left(\vec{l}\right)_{\text{CIP}} T^*\left(\vec{l'}\right)_{\text{CIP}} \right\rangle = \left(2\pi\right)^2 C_l^{TT} \delta^{(2)} \left(\vec{l} - \vec{l'}\right) + \left(2\pi\right)^2 \Delta \left(\vec{l} + \vec{l'}\right) \left. \frac{dC_{l'}^{TT}}{d\Omega_b} \right|_{\Omega_m}$$

Can be used to reconstruct CIP from Isotropy-breaking term in fixed CMB map! CIP realization

* Generate CIP map (reconstruction)

$$\hat{\Delta}_{LM} = \left(N_L^{\Delta\Delta}\right)^{-1} \int d\hat{n} Y_{LM}^*(\hat{n}) \overline{T}(\hat{n}) S(\hat{n}) + (1 \leftrightarrow 2)$$
$$\bar{T}(\hat{n}) = \sum_{lm} Y_{lm}(\hat{n}) \overline{T}_{lm}^{(a)},$$
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arXiv: 1306.4319 (DG, Duncan Hanson + ...)-Phys. Rev. D 89, 023006 (2014)



Upper limit to CIP spectrum at a variety of scales



Upper limit to CIP spectrum at a variety of scales



Cosmic baryon fraction is homogeneous at 10-20% level at 5-100° scales at z=1100!

Upper limit to CIP spectrum at a variety of scales



$A_L = 1.14 \pm 0.08$ $\Delta_{\rm rms}^2 \le 0.01$

Comparable limit from Planck power spectra (lower order statistic) Julian B. Muñoz, DG, Liang Dai, Ely Kovetz, Marc Kamionkowski arXiv: 1511.04441, Phys. Rev. D 93, 043008

COMPENSATED ISOCURVATURE AND THE CMB: FORECAST WITH RECONSTRUCTION



COMPENSATED ISOCURVATURE AND THE CMB: FORECAST WITH RECONSTRUCTION







Two orders of magnitude improvement: conservatively 45

COMPENSATED ISOCURVATURE AND THE CMB: FORECAST WITH RECONSTRUCTION



Ultimate reach of power-spectrum only (Gaussian) method Two orders of magnitude improvement: conservatively 45
COMPENSATED ISOCURVATURE AND THE CMB: FORECAST WITH RECONSTRUCTION



Naive curvaton target

Two orders of magnitude improvement: conservatively 45

* Most interesting curvaton scenario if baryon number generated by curvaton decay, CDM after

$$S_{m\gamma}^{\text{eff}} = S_{c\gamma} + \frac{\Omega_b}{\Omega_c} S_{b\gamma} \propto \left(r_{\text{D}} - \frac{\Omega_b}{\Omega_m} \right) \zeta$$

* Linear CMB isocurvature limits then require

 $r_{\rm D} = 0.160 \pm 0.005$

* Predicting ...

$$S_{bc} = A\zeta; \ A \simeq 19$$

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* Predicting

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Large, possibly detectable CIPs, correlated with adiabatic fluctuations

* Correlation of CIP and temperature fields

$$\left\langle \Delta^*(\vec{k}) \left\lfloor \frac{\Delta T(\vec{k}')}{T} \right\rfloor \right\rangle = -\frac{1}{5} \left\langle \Delta^*(\vec{k})\zeta \right\rangle = -\frac{A}{5} \left\langle \zeta^*(\vec{k})\zeta(\vec{k}') \right\rangle = -\left(2\pi\right)^3 \frac{A}{5} \delta^3(\vec{k} - \vec{k}') P_{\zeta\zeta}(k)$$

* Correlate two maps to estimate A

$$\hat{A} \propto \sum_{LM} \frac{\hat{\Delta}_{LM}^* T_{LM}}{2L+1} \propto \sum_{LMlml'm'} T_{LM} T_{lm}^* T_{l'm'} V_{lml'm'}^{LM}$$

C. He Heinrich, DG, and Wayne Hu



arXiv:1505.00369 PRD92, 063018

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Sachs-Wolfe (large-scale) CMB transfer function * Correlate two maps to estimate A

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C. He Heinrich, DG, and Wayne Hu arXiv:1505.00369

Weighting

PRD92, 063018



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3-pt function!

C. He Heinrich, DG, and Wayne Hu



arXiv:1505.00369 PRD92, 063018

OBSERVABILITY OF CURVATON-GENERATED CHIPS



Curvaton CIP amplitude is detectable



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OBSERVABILITY OF CURVATON-GENERATED CHIPS



Curvaton CIP amplitude is detectable

CONCLUSIONS

*****Ultra-light axions

 $*\sim1\%$ level constraints on horizon

*Lensing is very promising, as is tensor + iso combo

*Work to be done improving theory

*Curvaton-sourced isocurvature perturbations

*Existing constraints require fine tuning curvaton-decay scenario

*Some scenarios will be strongly probed by CIP measurements